# **B.Sc. MATHEMATICS**

# **SYLLABUS**

(with effect from June 2015)



# **DEPARTMENT OF MATHEMATICS**

The Gandhigram Rural Institute – Deemed University Gandhigram – 624 302 Tamil Nadu





# Gandhigram Rural Institute (Deemed University), Gandhigram - 624302

(Fully Funded by Ministry of Human Resource Development, Govt. of India)

# Department of Mathematics

B.Sc. Degree (Mathematics)

Revised Syllabus with effect from 2015 – 2016 onwards

Category	Course	Course Title	Number	Lecture	Exam		Marks	
	Code		of	Hours per	Duration	C.F.A	E.S.E	Total
			Credits	week	(Hrs)			
	Semester-I					T	T	
	15TAMU0101/	T T						
	15MALU0101/	Language I (Tamil/Hindi/Malayala	3	3	3	40	60	100
Language	15HIDU0101/	m/French)	3	3	3	40	00	100
	15FREU0101	in Teneny						
	15ENGU01X1	Language II	3	3	3	40	60	100
		English		_				
	15MATU0101	Classical Algebra	4	4	3	40	60	100
Core Course	15MATU0102	Theory of Equations & Trigonometry	3	3	3	40	60	100
	15PHYU01A1	Allied Physics –I (theory)	3	3	3	30	45	75
Allied Course	@	Allied Physics –I		3				
		(practical)		3			40 60 10  40 60 10  40 60 10  40 60 10  30 45 75   50 50  100 10  40 60 100  40 60 100	
	15NSSU0001/							
Foundation	15SHSU0001/	NCC/CC/EA/Cports	1	1		50		50
Course	15FATU0001/	NSS/SS/FA/Sports	1	1 -	) )0	_	30	
Gourse	15SPOU0001							
	15YOGU0002	Yoga	1	1	-	50	-	50
	15EVSU0001	Environmental Studies	3+1	3+2	-	100	-	100
		TOTAL	22					
	Semester-II							
	15TAMU0202/	Language I						
	15MALU0202/	(Tamil/Hindi/Malayalam	3	3	3	40	60	100
Language	15HIDU0202/ 15FREU0202	/French)						
Language	15ENGU02X2	Language II	3	3	3	40	60	100
		English			-			
	15CTAU0001/ 15CHIU0001	Core Hindi/Core Tamil	2	2	2	20	30	50

Core Course	15MATU0203	Calculus	4	4	3	40	60	100
Allied Course	15PHYU02A2	Allied Physics – II (theory)	3	3	3	30	45	75
7 mica douise	15PHYU02A3	Allied Physics – II (practical)	2	3	3	30	20	50
Foundation	15GTPU0001	Gandhi's Life, Thought and Work	2	2	2	20	30	50
Course	15EXNU0001	Extension Education	2	2		20	30	50
Soft Skill	15ENGU00C1	Communication and Soft Skills	2	2		20	30	50
		TOTAL	23					
	Semester-III							
I an aveca	15TAMU0303/ 15MALU0303/ 15HIDU0303/ 15FREU0303	Language I (Tamil/Hindi/Malayala m/French)	3	3	3	40	60	100
Language	15ENGU03X3	Language II English	3	3	3	40	60	100
	15CTAU0002 / 15CHIU0002	Core Hindi/ Core Tamil	2	2	2	20	30	50
Core Course	15MATU0304	Sequences, Series & Vector Calculus	3	3	3	40	60	100
	15MATU0305	Analytical Geometry	4	4	3	40	60	100
Allied Course	15MATU03A1	Object Oriented Programming with C++ Theory	3	3	3	30	45	75
	15MATU03A2	Object Oriented Programming with C++ Practical	1	2	3	15	10	25
Computer Skill	15MATU0306	Introduction to Computers and Office Automation (theory)	3	3	3	30	45	75
	15MATU0307	Introduction to Computers and Office Automation (practical )	1	2	3	15	10	25
Extension	15EXNU03V1	Village Placement Programme	2			50		50

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Compulsory		Compulsory Non Credit						
Non Credit	15MATU00F1	Course		2	-	50	-	
Course		(Extension / Field Visit)						
		TOTAL	25					
	Semester – IV							
Core Course	15MATU0408	Abstract Algebra	4	4	3	40	60	100
Core Course	15MATU0409	Mathematical Statistics	4	4	3	40	60	100
	15MATU0410	Mechanics	4	4	3	40	60	100
Allied Course	15MATU04A3	Programming with Java Theory	3	3	3	30	45	75
Affied Course	15MATU04A4	Programming with Java Practical	1	2	3	15	10	25
Electives	15MATU04EX	Major Elective	3	3	3	40	60	100
Electives		Non Major Elective	3	3	3	40	60	100
Compulsory Non Credit Course	15MATU00F2	Compulsory Non Credit Course Extension / Field Visit		2				
		TOTAL	22					
	Semester – V							
	15MATU0511	Modern Analysis	4	4	3	40	60	100
Core Course	15MATU0512	Linear Algebra	4	4	3	40		100
	15MATU0513	Linear Programming	4	4	3	40	60	100
T1	15MATU05EX	Major Elective	3	3	3	40	60	100
Electives		Non Major Elective	3	3	3	40	60	100
Skill Based Elective	15MATU05S1	Quantitative Skills	2	2		20	30	50
		TOTAL	20					
	Semester – VI					<u>'</u>		
	15MATU0614	Operations Research	4	4	3	40	60	100
Core Course	15MATU0615	Differential Equations	4	4	3	40	60	100
	15MATU0616	Complex Analysis	4	4	3	40	60	100
	15MATU0617	Graph Theory	3	3	3	40	60	100
	15MATU06MX	Modular Course	2	2		50		50
Modular Course			2	2		50		50
Project	15MATU0618	Project	4	8		40	40+20	100
,		TOTAL	23					
	(	GRAND TOTAL	136				<u> </u>	
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# MAJOR ELECTIVES:

(15MATU04EX/ 15MATU05EX)

# Semester -IV

- 1. 15MATU04E1 Numerical Methods
- 2. 15MATU04E2 Financial Mathematics

# MODULAR COURSES: (15MATU06MX)

# Semester -V

- 1. Fuzzy Set Theory
- 2. Mathematical Skills
- 3. Advanced Statistics

# Semester -V

- 1. 15MATU05E1 Discrete Mathematics
- 2. 15MATU05E2 Introduction to Actuarial Science

Core Course	Semester I	
15MATU0101	CLASSICAL ALGEBRA	Credits: 4

**Objective:** To impart skills in the various applications of algebraic methods.

#### Specific outcome of learning:

- The learner will become proficient in expansion and summation of function
- The learner will acquire knowledge of solving problems in matrices
- The learner will acquire skills of basic concepts of set theory
- The learner will become proficient in various types of functions
- The learner will acquire knowledge of basic concepts of number theory

**Unit 1:** Binomial theorem for any rational index - Exponential and Logarithmic Series - Summations and Approximations related to these series.

**Unit 2:** Matrices: Definition - Properties - Elementary transformations - Diagonalisation of matrices- Characteristic Equation - Cayley Hamilton Theorem - Evaluation of Eigen values and Eigen vectors.

**Unit 3:** Concept of a set- Finite and Infinite set – Axiom of extension – Set Algebra – Cartesian product of sets.

**Unit 4:** Relations and their types – Functions and their types-Countable and Uncountable sets.

**Unit 5:** Number Theory: Prime Numbers and Composite Numbers - Euler's function - Divisibility and Congruence relations - Fermat's theorem - Wilson's theorem.

# **Text Books:**

- 1. S. Narayanan& T. K. ManickavasagamPillai, **Algebra**, vol. 1, S. Viswanathan Pvt. Ltd., Chennai, 2004. Unit 1: Chapter 3, 4, 5.
- 2. S. Narayanan& T. K. ManickavasagamPillai, **Algebra**, Vol. 2, S. Viswanathan Pvt. Ltd. Chennai, 2004. Unit 2: Chapter 2. Unit 5: Chapter 5.
- 3. S. Narayanan & T. K. ManickavasagamPillai, **Modern Algebra**, Vol. 1, S. Viswanathan Pvt. Ltd. Chennai, 1999.Unit 3, 4: chapter: 2.

- 1. Seymour Lipschutz, **Set theory & Related Topics**, Schaum'soutlines, 2<sup>nd</sup> Edition, Tata McGraw Hill, New Delhi, 2005.
- 2. Arumugam&Issac, Classical Algebra, New gamma Publishing house, Tirunelveli, 2003.

Core Course	Semester I	
15MATU0102	THEORY OF EQUATIONS AND TRIGONOMETRY	Credits: 3

**Objective:** To learn techniques of solving algebraic and trigonometric equations.

#### Specific outcome of learning:

- The learner will acquire basic concepts of roots and coefficients of equation
- The learner will acquire skills of solving problems in transformation of equations
- The learner will gain knowledge of trigonometric functions and related problems
- The learner will become proficient in various types of hyperbolic functions
- The learner will acquire skills of solving problems in summations of trigonometric series

**Unit 1:** Theory of Equations: Fundamental Theorem of Algebra - Relations between roots and coefficients - Symmetric functions of roots.

**Unit 2:** Transformation of Equations - Reciprocal Equations - Newton's Method of Divisors - Descartes' rule of signs - Horner's Method.

**Unit 3:** Trigonometry: Expansion of functions,  $sin\ nx$ , cosnx,  $tan\ nx$  - Series for  $sin\ x$ ,  $cos\ x$ ,  $tan\ x$ ,  $sin^nx$  and  $cos^nx$  - Properties and their related problems.

**Unit 4:** Hyperbolic functions -Inverse hyperbolic functions- Logarithm of Complex Numbers.

**Unit 5:** Summations of trigonometric series- Properties and their related problems.

#### Text Books:

- 1. S. Narayanan & T. K. ManickavasagamPillai, **Algebra**, Vol. 2, S. Viswanathan Pvt. Ltd., Chennai, 2004. Unit 1: Chapter 6, Secs 6.1-6.14, Unit 2: Chapter 6, Secs 6.15-6.30.
- 2. S. Narayanan & T. K. ManickavasagamPillai, **Trigonometry**, S. Viswanathan Pvt. Ltd., Chennai, 2001. Unit 3: Chapter 3, Unit 4: Chapter 4, 5, Unit 5: Chapter 6.

#### Reference:

1. Arumugam&Issac, **Theory of Equations, Theory of Numbers and Trigonometry**, New gamma Publishing house, Tirunelveli, 2011.

Core Course	Semester II	
15MATU0203	CALCULUS	Credits: 4

**Objective:** To learn the different concepts of differential and integral calculus.

#### Specific outcome of learning:

- The learner will gain knowledge of differentiation and its applications
- The learner will acquire basic knowledge of integration
- The learner will become proficient in multiple integrals
- The learner will acquire skills of applications of multiple integrals
- The learner will gain concepts of change of variables

**Unit 1:** Differential Calculus: Successive Differentiation - Leibnitz theorem and its applications - Curvature - Radius of Curvature and Centre of Curvature - Evolutes and Involutes.

**Unit 2:**I ntegral Calculus: Properties of definite integrals - Integration by parts - Reduction formulae - Bernoulli's formula.

**Unit 3:** Integration as limit of an infinite sum. Multiple Integrals: Definition of double integral - Evaluation of double integral - double integral in polar coordinates.

**Unit 4:** Triple integrals. Improper Integrals: Beta and Gamma integrals and their relations.

**Unit 5:** Change of Variables: Jacobian - Change of variable in the case of two variables and three variables - Transformation from Cartesian to polar coordinates - Transformation from Cartesian to spherical polar coordinates.

#### Text Books:

- 1. S. Narayanan & T. K. Manickavasagam Pillai, **Calculus**, Vol.1. S. Viswanathan Pvt. Ltd., Chennai, 2004. Unit 1: Chapter III, Chapter X Secs 10.2.1-10.3.1
- 2. S. Narayanan & T. K. Manickavasagam Pillai, **Calculus,** Vol.2. S. Viswanathan Pvt. Ltd., Chennai, 2004. Unit 2: Chapter 1 Secs 1.1.1-1.15.1, Unit 3: Chapter I Secs 1.15.2, Chapter 5 Secs 5.1-5.3.2, Unit 4: Chapter 5 Secs 5.4-5.5.4 Chapter 7 Secs 7.1.1-7.5, Unit 5: Chapter 6

- 1. George B. Thomas, JR &Ross L. Finney, Calculus and Analytic Geometry, Sixth edition, Narosa Publishing House, New Delhi, 1986.
- 2. Arumugam & Isaac, Calculus, Vol. 1&2, New Gamma Publishing House, 1999.

Core Course	Semester III	
15MATU0304	SEQUENCES, SERIES AND VECTOR CALCULUS	Credits: 3

**Objective:** To enhance basic skills in the areas of sequences and vectors.

Specific outcome of learning: The learner will become proficient in

- Types of sets, inequalities and sequences
- Behavior of sequences and its subsequences
- Infinite series and various tests for finding its convergence
- Vectors and its product
- Multiple vector integration

**Unit 1:** Sequences: Sets and functions-Intervals in R-Bounded sets-Least upper bound and Greatest lower bound-Countable sets-uncountable sets-Inequalities of Holder's and Minkowski's-Bounded functions-Sequences-Bounded sequences-Monotonic sequences-Convergent sequences-Divergent and oscillating sequences- The algebra of limits.

**Unit 2:** Behaviour of monotonic sequences-Some theorems on limits-Subsequences-Limit points-Cauchy sequences-The upper and lower limit of a sequence.

**Unit 3:** Series of positive terms: Infinite series-Comparison test-Kummer's test -Root test and condensation test-Integral test-Series of arbitrary terms: Alternating series-Absolute convergence.

**Unit 4:** Vector Differentiation: Introductory Ideas-Vector Products-Gradient-Divergence - Curl.

**Unit 5:** Vector Integration: Line integral-Volume integral-Surface integral –Gauss divergence theorem(without proof) -Stoke's theorem (without proof) – Green's theorem (without proof). **Text Books:** 

- 1. S. Arumugam& A. Thangapandi Isaac, **Sequences and series**, New Gamma Publishing House, Palayamkottai, 1999.Unit 1-Secs 1.1-1.5, 3.1-3.6, Unit 2-Secs 3.7-3.12, Unit 3-Secs 4.1-4.5, 5.1-5.2.
- 2. S. Arumugam& A. Thangapandi Isaac, **Modern Analysis**, New Gamma Publishing House, Palayamkottai, 2002.Unit 1-Secs 1.2-1.4
- 3. S. Narayanan & T. K. ManicavachagomPillai, **Vector Algebra and Analysis**, S.Viswanathan Pvt. Ltd., Chennai, 1995.Unit 4- Chapters 1, 2, 4, Unit 5- Chapter 6.

- 1. N. P. Bali, **Real Analysis**, An imprint of Laxmi Publications Pvt. Ltd., New Delhi, 2005.
- 2. Sterling K. Berberian, A First Course in Real Analysis, Springer, New York, 2004.
- 3. Robert G. Bartle, Donald R. Sherbert, **Introduction to Real Analysis**, John Wiley and Sons, New Delhi, 1982.

Core Course	Semester III	
15MATU0305	ANALYTICAL GEOMETRY	Credits: 4

**Objective:** To study the various properties of geometrical figures in two dimension and three dimension.

#### **Specific outcome of learning:** The learner will

- understand the basic concepts of circles, parabola, ellipse and hyperbola as a 2 dimensional objects.
- acquire knowledge of representing conics in polar co-ordinates.
- acquire knowledge of planes and its properties as a 3 dimensional objects.
- understand the concepts skew lines and spheres.
- solving problems related to geometry of two dimension and three dimension.

**Unit 1:** System of circles: orthogonal circles - coaxal systems- properties and related problems. Parabola: properties and related problems.

**Unit 2:** Ellipse – Hyperbola – Properties-and their related problems.

**Unit 3:** Polar Equations: Representation of basic curves in polar coordinates. General equation of Conic: Tracing the Conic - Properties and its applications.

**Unit 4:** Basic Properties – Direction Ratios and Direction Cosines – General equations of Plane – normal form- plane through the line of intersection of two planes.

**Unit 5:** Equation of the straight line – coplanar lines – skew lines – intersection of three planes. Sphere – Standard equation – properties and related problems.

#### **Text Books:**

- 1. S. Narayanan & T. K. ManickavasagamPillai, **Analytical Geometry 2D**, S. Viswanathan Pvt. Ltd., Chennai, 2001.Unit 1: Chapter V, VI, Unit 2: Chapter VII, VIII, Unit 3: Chapter IX (up to section 9), X (up to section 8)
- 2. S. Narayanan & T. K. ManickavasagamPillai, **Analytical Geometry 3D**, S. Viswanathan Pvt. Ltd., Chennai, 2001.Unit 4: Chapter I, II, Unit 5: Chapter III, IV

- 1. George B. Thomas, JR & Ross L.Finney, Calculus and Analytic Geometry, Sixth edition, Narosa Publishing House, New Delhi, 1986.
- 2. S. Arumugam&Issac, **Analytical Geometry 3D and Vector Calculus**, New Gamma Publications Palayamkottai, 1997.

Allied Course -Theory	Semester III	
15MATU03A1	OBJECT ORIENTED PROGRAMMING WITH C++	Credits: 3

**Objective:** To develop programming skills in C++ and its object oriented concepts.

# Specific outcome of learning:

- The learner will become proficient in object oriented programming concept and proficient in C++ tokens
- Proficient in C++ operators
- Proficient in C++ class declaration and definition and its objects
- Proficient in constructors, destructors and operator overloading
- Proficient in the concept inheritance

**Unit 1:** What is C++ - Applications of C++ - A simple C++ program - An example with class - tokens - keywords - Identifiers and constants - basic, user defined, derived data types-symbolic constants - type compatibility - declaration of variables - dynamic initialization of variables.

**Unit 2:** Operator in C++ - scope resolution, member differencing, memory management operators - manipulators - type cast operator - the main function - function prototyping - call by reference - return by reference - inline functions - default, constant arguments - function overloading - math library functions.

**Unit 3:** C structure - specifying a class - defining member function - a C++ program with class making an outside function inline - nesting of member function - private member function - array within class - static data members - static member functions - array of objects -objects as function arguments - friendly functions

**Unit 4:** Constructors – parameterized constructors - multiple constructors in a class - constructors with default arguments - dynamic initialization of objects - copy constructor - dynamic constructors – destructors - defining operator overloading - overloading unary, binary operators.

**Unit 5:** Defining derived classes - single inheritance - multilevel inheritance - multiple inheritance-hierarchical inheritance -hybrid inheritance - virtual base class - abstract classes - constructors in derived classes.

# **Text Book:**

1. E. Balagurusamy, **Object Oriented Programming with C++,** Third edition, Tata McGraw-Hill publication, New Delhi, 2006.

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Unit 1: Chapters: 2.1 - 2.5, 3.1- 3.11, Unit 2: 3.13-3.18, 4.1-4.9 & 4.11. Unit 3: 5.1- 5.9, 5.11-5.15. Unit 4: 6.1-6.8, 6.11, 7.2-7.5. Unit 5: 8.1-8.11.
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- 1. V. Ravichandran, **Programming with C++,** Second Edition Tata McGraw Hill, New Delhi, 2006.
- 2. H. Schildt, **The complete Reference of C++,** Tata-McGraw-Hill publishing Company Ltd. New Delhi, 2003.

Allied Course -Practical Semester III
15MATU03A2 OBJECT ORIENTED PROGRAMMING WITH C++ Credit: 1

# Practical related to Object Oriented Programming with C++

- 1. List the prime numbers in a given range
- 2. Display Fibonacci series
- 3. Sorting given list of names in alphabetical order
- 4. Sorting given list of numbers in ascending order
- 5. Read and display for a given matrix of any order
- 6. Compute simple and compound interest values
- 7. Computer biggest among three numbers
- 8. Compute biggest among N integers
- 9. Compute factorial of a given number using recursive function
- 10. Write a program to swap the values using functions
- 11. Print perfect squares in a given range
- 12. Write a program to solve a quadratic equation and test with three types of roots.
- 13. Write a program to calculate the following functions to 0.0001% accuracy

a) 
$$\sin x = x - \frac{x^3}{3!} + \frac{x^5}{5!} - \cdots$$

b) 
$$SUM = 1 + \left(\frac{1}{2}\right)^2 + \left(\frac{1}{3}\right)^3 + \left(\frac{1}{4}\right)^4 + \cdots$$

c) 
$$\cos x = 1 - \frac{x^2}{2!} + \frac{x^4}{4!} - \cdots$$

- 14. Write a program to calculate variance and SD of N numbers
- 15. Write a program to read two matrices and compute matrix multiplication using functions
- 16. Prepare employee details using class with array of objects
- 17. Program to illustrate objects as function arguments
- 18. Program to illustrate parameterized constructors
- 19. Program to illustrate multiple constructors in a class
- 20. Show by a suitable program: how the unary minus operator is overloaded?
- 21. Show by a suitable program: how the binary operator is overloaded?
- 22. Prepare student mark list by using multilevel inheritance
- 23. Program to illustrate multiple inheritance
- 24. Prepare student mark list by using hybrid inheritance
- 25. Prepare student mark list by using the concept of virtual base class

# Core Course- Theory Semester III 15MATU0306 INTRODUCTION TO COMPUTERS AND OFFICE AUTOMATION Credits: 3

**Objective:** To gain basic knowledge about computer peripherals, MS Office, Internet and E-commerce.

# Specific outcome of learning:

- The learner will become proficient in MS windows software
- The learner will become proficient in MS word
- Proficient in data representation in diagram via MS Excel
- Proficient in preparation of power points
- Proficient in creation of E-mail and uses of web browser

**Unit 1:** Introduction to Computer: Block diagram, Memories, Devices, Operating System, Devices. Introduction to Windows: Starting Windows - Desktop - closing Windows - Start button - icons - Task bar - shortcut icons. Windows properties - Menu options, Minimize, Maximize, Close Active & Inactive Windows - Personal tools. Word pad: Creating &Saving a file, opening the saved file, word processing. Paint: creating & editing bitmaps - Multimedia tools - file system. Hard disk: Drive - folders - file - Exploring the files. My Computer - Explorer - moving files, deleting, cut, copy, paste - Exploring web.

**Unit 2:** Word Processing using MS WORD: Word processing - Advantages - MS WORD - Definition. Document: Create - save - Printing - Resave - Close- Exiting word. Editing: Opening document - cursor movement - selecting text - deleting - undo redo - Moving text - Copying text. Formatting text: Font - paragraph formatting - bullets & numbering - getting help - find and replace text - spell checking and correction - grammar checking - auto correct - auto text - using thesaurus - using tabs - defining & changing page setup - page print options. Tables: creating &formatting, multiple columns. Math equations and type setting in MS Word.

**Unit 3:** MS-EXCEL: Introduction to worksheet and Excel - Definitions - Advantages - Organization of worksheet area - entering information - number - Formula - save - data alignment - editing - range -definition - specifying - changing column width - row height - centering cell across column, hiding columns and rows - moving and copying data - inserting and deleting rows and columns - getting help.

**Unit 4:** MS-EXCEL: Formatting the worksheet - printing - setting up page and margin-defining header and footer - print options. Chart: creation - changing type - resize and move – controlling the appearance - modifying - deleting - printing - naming ranges - using statistical, Mathematical and financial functions - using drawing tool bar.

**Unit 5:** MS-POWER POINT: Introduction - Menus - Toolbar - Navigating Power Point—Creating Slides, Presentation, Animation, etc - working with Power Point. Internet: Internet Browsing, creating mail ID, Using search engines etc. — To know important govt. webpage's for various forms, formats, exams etc, National/International University/Institute websites.

#### **Text Book:**

1. Sanjay Saxena, **MS-Office -2000 for every one**, Vikas Publishing House Pvt. Ltd., New Delhi, 2000.

Unit 1: Part I, Unit 2: Part II, III, Unit 3, 4: Part IV, Unit 5: Part V.

#### Reference:

1. R.X. Taxali, **P.C. Software for Windows 98 Made simple**, TATA McGraw-Hill Publishing Company Ltd., New Delhi, 2001.

Core Course-Practical Semester III
15MATU0307 INTRODUCTION TO COMPUTERS AND OFFICE AUTOMATION Credit: 1

#### Practical related to Computer Skill

- 1. Note pad Applications
- 2. Control Panel Setup
- 3. Designing Advertisement and Document creation with special features like header, footer, tables, etc.
- 4. Typing practices on Algebraic & Transcendental Equations, System of Equations, Matrices, Integral Equations, Differential Equations, etc. in MS Word
- 5. Table creation and Table editing, Table to Text / Text to Table conversion in MS Word
- 6. Electricity Bill creation, Mark sheet creation and Charts in Work Sheet
- 7. Power Point presentation on various concepts
- 8. Regression Equation Worksheet

Core Course	Semester IV	
15MATU0408	ABSTRACT ALGEBRA	Credits: 4

**Objective:** To provide some knowledge about various algebraic structures.

**Specific outcome of learning:** The learner will be able to

- recognize the basic properties of groups and subgroups.
- understand the types of homomorphism and use them to classify groups.
- apply the theorems to study the structure of groups.
- recognize the basic properties of rings, fields and integral domains.
- apply the algebraic methods for solving problems.

**Unit 1:** Groups: Definition and Examples - Elementary Properties of a group - Quaternion group - Groups of symmetries - Order of an element - Sub groups.

**Unit 2:** Homomorphism and their types – Cayley's theorem – Groups of permutations-Cyclic groups.

**Unit 3:** Automorphisms – Cosets and Lagrange's theorem – Normal subgroups and Quotient groups – Fundamental theorem of Homomorphism.

**Unit 4:** Rings: Definition and Examples – Elementary Properties of rings –Division rings and Fields – Ordered Integral Domain – Sub rings and sub fields.

**Unit 5:** Homomorphism of rings and their types – Ideals – Quotient Structure and Isomorphism theorems – Fundamental theorem of ring Homomorphism – Prime and Maximal Ideals.

#### **Text Book:**

1. S. Narayanan & T. K. ManickavasagamPillai, **Modern Algebra**, Vol. II, S. Viswanathan Pvt. Ltd., Chennai, 1997.

Unit 1: Chapter 1: Sections 1.1, 1.2, 1.3

Unit 2: Chapter 1: Sections 1.4, 1.5, 1.6

Unit 3: Chapter 1: Sections 1.7, 1.8, 1.9, 1.10 (up to Theorem 1.10.3)

Unit 4: Chapter 2: Sections 2.1, 2.2, 2.3, 2.4

Unit 5: Chapter 2: Sections 2.5, 2.6, 2.7, 2.8

- 1. S. Arumugam& A. T. Isaac, Modern Algebra, SciTech Publications, India Pvt. Ltd., 2003.
- 2. John. B. Fraleigh, **A first course in abstract algebra**, 7<sup>th</sup> edition, Addison-Wesley Publications, US, 2003.

Core Course	Semester IV	
15MATU0409	MATHEMATICAL STATISTICS	Credits: 4

**Objective:** To impart skills in various applications of statistical methods.

### **Specific outcome of learning:** The learner will be able to

- analyze the given data by using statistical methods.
- understand the basic concepts of probability and related results.
- use different probabilistic methods to solve problems arise in different situations.
- construct and evaluate hypothesis tests.
- apply sampling techniques to real life situations.

**Unit 1:** Measures of Central Tendency – Measures of Dispersion – Moments, Skewness and Kurtosis – Theory of Probability: Definition – Axioms – Addition and Multiplication Theorems –Baye's Theorem on conditional probability and its applications.

**Unit 2:** Random variables – Discrete and Continuous – Definition of Probability Mass Function and Density Function – Distribution Functions – Properties – Mathematical Expectations – Mean, Variance and Moments – Moment Generating Functions – Simple properties .

**Unit 3:** Theoretical distributions – Discrete: Binomial Distribution and Poisson distribution – Continuous: Normal Distribution Properties and Applications.

**Unit 4:** Curve Fitting by the Method of Least Squares – Correlation – Properties – Regression – Equations of Regression Lines – Angle between Regression Lines – Properties and Applications.

**Unit 5:** Sampling: Introduction — Types of Sampling — Parameters and Statistical Tests of Significance — Null Hypothesis — Large Sample Tests — Sampling Distributions: t, Chi — Square and F distributions.

#### Text Book:

1. S. Arumugam& A. Thangapandi Isaac, **Statistics**, New Gamma Publishing House, 2006.

Unit 1: Chapter 1: Sections 1.0 -1.4; Chapter 2: Section 2.0-2.5; Chapter 3: Sections: 3.0

-3.2; Chapter 4: Sections: 4.0 -4.2; Chapter 11: Sections: 11.0 -11.2.

Unit 2: Chapter 12: Sections 12.0 -12.5.

Unit 3: Chapter 13: Sections 13.0-13.3.

Unit 4: Chapter 5: Section 5.0, 5.1; Chapter 6: Section 6.0-6.3

Unit 5: Chapter 14: Sections 14.0-14.5.

- 1. J.N. Kapoor& H.C. Saxena, **Mathematical Statistics**, S. Chand & Co Pvt. Ltd., New Delhi, 1994.
- . S. C. Gupta & V. K. Kapoor, **Fundamentals of Mathematical Statistics**, S. Chand & Sons Pvt. Ltd., New Delhi, 1994.

Core Course	Semester IV	
15MATU0410	MECHANICS	Credits: 4

**Objective:** To learn the application of geometric and trigonometric properties in equilibrium and motion of particles.

# Specific outcome of learning:

- The learner will be able to apply geometrical concepts in parallel forces, moments and couples
- Proficient in static equilibrium of three forces acting on a rigid body and friction
- Proficient in Newton's laws of motion and projectiles
- Proficient in collision of elastic bodies
- Proficient in motion under action of central forces

**Unit 1:** Basic Concepts and Principles - Forces acting at a Point - Lami's Theorem and Applications - Parallel Forces - Like and Unlike Parallel Forces - Moment of a force - Couples - Related problems.

**Unit 2:** Equilibrium of Three Forces acting on a rigid body - Friction - Laws of Friction - Angle of Friction - Cone of Friction - Properties and related problems.

**Unit 3:** Motion in a Straight line under uniform acceleration - Newton's Laws of motion. Projectiles: Definition - Path of Projectile - Range on an Inclined Plane - Properties and Problems.

**Unit 4:** Impulse and Impact: Collision of Elastic Bodies – Direct and Oblique Impact – Loss of Kinetic Energy – Related Properties and Simple Problems.

**Unit 5:** Central Orbits: Motion under the action of Central Forces - Properties and Related Problems - Differential Equation of Central Orbit - Pedal Equation of Central Orbit - Velocities in a Central Orbit - Law of Forces - Properties and Related Problems.

#### **Text Books:**

1. M. K. Venkataraman, **Statics**, Agasthiar Publications, Trichy, 2004.

Unit 1: Chapters 2, 3, 4

Unit 2: Chapters 5, 7

2. M. K. Venkataraman, **Dynamics**, Agasthiar Publications, Trichy, 2004.

Unit 3: Chapters 3: section 3.22, Chapter 4: Section 4.3, Chapter 6

Unit 4: Chapter 8

Unit 5: Chapter 11

- 1. T. K. ManickavasagamPillai, Statics, S. Viswanathan& Co., Chennai, 1980.
- 2. S. Narayanan, **Dynamics**, S. Chand & Co., New Delhi, 1980.

Allied Course -Theory 15MATU04A3

# Semester IV PROGRAMMING WITH JAVA

Credits: 3

**Objective:** To develop object oriented programming skills in JAVA and its applications in webpage designing.

# Specific outcome of learning:

- The learner will become proficient in the creation and implementation of java programs and Java tokens
- Proficient in operators and expressions
- Proficient in decision making and looping
- Proficient in interfaces
- Proficient in applet programming

**Unit 1**: Overview of java language: Introduction - Simple java program - An application with two classes - Java program structure - Java tokens - Java statements - implementing a java program - Java virtual machine - Command line arguments: Constants, Variables and Data types - declaration of variables giving values to variables - Scope of variables - Symbolic constants - Type casting - Getting values of variables - Standard default values.

**Unit 2:** Operators and Expressions: Arithmetic operators - Relational operators - Logical operators - Assignment operators - Increment and decrement operators- Conditional operators - Bitwise operators - Special operators - Arithmetic expressions - Evaluation of expressions - Precedence of Arithmetic operators - Type conversion in expressions - Operator precedence and associativity. Decision making and Branching: Decision making with if statement - Simple if statement - The if....else statement - Nesting of if else statements - The else if ladder - Switch statement - The?: operator.

**Unit 3:** Decision making and Looping: The while statement - The do statement - the for statement - Jumps in loops - Labeled loops. Classes, Objects and Methods Defining a Class - Adding variables -. Adding methods - Creating Objects - Accessing Class members - Constructors - Methods. Overloading - Static members - Nesting of methods - Inheritance: Extending a class - Overriding methods - Final variables and methods - final classes - finalizer methods - Abstract methods and, classes - visibility control - Arrays - One dimensional. Arrays - Crating an array - Two dimensional array - Strings - Vectors - wrapper Classes.

**Unit 4:** Interfaces: Defining interfaces - Extending interfaces - Implementing interfaces - Accessing interface variables - Packages: Java API Packages - Using system packages - Naming conventions - Creating packages - Accessing a package - Using a package - adding a class to a package - Hiding classes.

**Unit 5:** Applet Programming: Introduction - How applets differ from applications - Preparing to write applet - Building applet code - Applet life cycle - Creating an executable applet - Designing a web page - Applet tag - Adding applet to HTML File - Running The Applet - More about applet tag - Displaying numerical values- Getting input from the user. Graphics Programming: Introduction - The Graphics class - Lines and Rectangles - Circles and Ellipses - Drawing arcs - Drawing polygons -. Line graphs - Using control loops in applets - Drawing bar charts.

#### **Text Book:**

1. E.Balagurusamy, **Programming with Java**, McGraw - Hill Publishing Company Ltd., New Delhi, 2005.

Unit 1: Chapters 3, 4

Unit 2: Chapters 5, 6

Unit 3: Chapters 7, 8, 9

Unit 4: Chapters 10, 11

Unit 5: Chapters 14, 15.

- 1. H. Sehildt, **JAVA2: The Complete Reference**, Fourth Edition, TMH Publishing Company, New Delhi, 2001.
- 2. C. Xavier, Programming with JAVA 2, SciTech Publications, Chennai, 2000.

Allied Course -Practical Semester IV
15MATU04A4 PROGRAMMING WITH JAVA Credit: 1

# Practical related to Programming with Java

- 1. Write a program to determine the sum of harmonic series
- 2. Write a program to convert the given temperature in Fahrenheit to Celsius
- 3. Write a program to perform any 5 math functions
- 4. Write a program to solve two linear equations with two unknowns
- 5. Prepare your house EB bill according to unit price of reading range by TNEB
- 6. Display Floyd's triangle
- 7. Compute power of 2 using for loop
- 8. Reverse the digits using while loop
- 9. Write a program that computes and prints a table of factorials for any given m.
- 10. Write a program to compute sum of digits of a given integer
- 11. Write a program using do....while loop to calculate and print first m Fibonacci numbers
- 12. Program to illustrate Class
- 13. Program to illustrate Constructors
- 14. Program to illustrate method overloading
- 15. Program to illustrate static members
- 16. Program to illustrate inheritance concept
- 17. Write a program to sort a list of numbers
- 18. Write a program to perform matrix multiplication
- 19. Write a program for alphabetical ordering of strings
- 20. Write a program to calculate compound interest value by using wrapper class methods
- 21. Prepare student mark list by implementing multiple inheritance using interfaces
- 22. Program to illustrate packages
- 23. Develop an applet that receives three numeric values as input from the user and then displays the largest value on the screen. Write a HTML page and test the applet.
- 24. Applet program to display bar chart for the following data:

Year : 2010 2011 2012 2013 2014 2015 Turnover : 110 150 100 170 190 120

(Rs. Crores)

- 25. Write applets to draw the following shapes:
  - a) Cone
  - b) Cylinder
  - c) Cube
  - d) Square inside a circle
  - e) Circle inside a square

Core Course	Semester V	
15MATU0511	MODERN ANALYSIS	Credits: 4

**Objective:** To impart concepts about sets with metric and related properties.

Specific outcome of learning: The learner will become proficient in

- Sets with various metric functions
- Open sets and closed sets and its properties
- Completeness of a metric space
- Continuous and discontinuous functions on metric spaces
- Connected metric spaces and properties of continuous functions on it

**Unit 1:** Metric Spaces: Definitions and examples-Bounded sets in a metric space-Open ball in a metric space-Open sets-equivalent metrics.

**Unit 2:** Subspaces- Interior of a set- Closed sets –Closure- Limit point-Dense sets.

**Unit 3:** Complete metric space: Completeness- Cantor's intersection theorem-Baire's Category theorem.

**Unit 4:** Continuity: Continuity – Homeomorphism-Uniform continuity-Discontinuous functions on R.

**Unit 5:** Connectedness: Definition and examples, Connected subsets of R- Connectedness and continuity; Compact space: Compact subsets of R-Equivalent characterization for compactness- Compactness and continuity.

#### Text Book:

1. S. Arumugam& A. Thangapandi Isaac, **Modern Analysis**, New Gamma Publishing House, Palayamkottai, 2002.Unit 1-Secs 2.1-2.4. Unit 2-Secs 2.5-2.10. Unit 3-Secs 3.1-3.2. Unit 4-Secs 4.1-4.4. Unit 5-Secs 5.1-5.3, 6.1-6.4.

- 1. N. P. Bali, **Real Analysis**, An imprint of Laxmi Publications Pvt. Ltd., New Delhi, 2005.
- 2. Sterling K. Berberian, A First Course In Real Analysis, Springer, New York, 2004.
- 3. Robert G. Bartle and Donald R. Sherbert, **Introduction to Real Analysis**, John Wiley and Sons, New Delhi, 1982.
- 4. Richard R. Goldberg, **Methods of Real Analysis**, Oxford & IBH Publishing CO. PVT. LTD., New Delhi, 1970.
- 5. S. C. Malik &SavitaArora, **Mathematical Analysis**, New Age International LTD., New Delhi, 1992

Core Course	Semester V	
15MATU0512	LINEAR ALGEBRA	Credits: 4

**Objective:** To introduce the fundamentals of Vector spaces.

**Specific outcome of learning:** The learner will be able to

- recognize the basic properties of vector spaces
- understand the concepts of linear algebra in geometric point of view
- visualize linear transformations as a matrix form
- apply the tools of linear algebra to solve the system of equations
- formulate the importance and applications of linear algebra in many branches of mathematics

**Unit 1:** Vector Spaces: Definition and Examples –Properties of vector space - Linear combination-Linear span.

Unit 2: Linear Dependence and Independence–Basis- Dimension- Quotient space.

**Unit 3:** Isomorphism of vector spaces – Direct sums- Matrix of a linear transformation-Rank and Nullity of a linear transformation.

**Unit 4:** Characteristic equation of a matrix- Matrix Polynomial – Elementary matrices and Transformations- Row rank, column rank and rank of a matrix- Row space and column space.

**Unit 5:** Inner product spaces: Definition and Examples –Orthogonality – Orthogonalization-Orthogonal Complement.

#### Text Book:

1. S. Narayanan & T. K. ManickavasagamPillai, **Modern Algebra**, Vo1 III, S. ViswanathanPvt. Ltd., Chennai, 1997.

Unit 1: Chapter 1: Sections 1.1, 1.2, 1.3, 1.4.

Unit 2:Chapter 1: Sections 1.5, 1.6, 1.7, 1.8.

Unit 3:Chapter 1: Sections 1.9, 1.10; Chapter 2: Sections 2.1, 2.2.

Unit 4:Chapter 2: Sections 2.5, 2.6, 2.7.

Unit 5:Chapter 3: Sections 3.1, 3.2, 3.3, 3.4

- 1. S. Arumugam&A. T. Isaac, Modern Algebra, SciTech Publications, India Pvt. Ltd., 2003.
- 2. S. Kumaresan, Linear Algebra: A Geometric approach, Prentice Hall of India, 2006.
- 3. VivekSahai&VikasBist, **Linear Algebra**, Narosa Publishing House, 2002.

Core Course	Semester V	
15MATU0513	LINEAR PROGRAMMING	Credits: 4

**Objective:** To impart the basic concepts and applications of linear programming. **Specific outcome of learning:** 

- The leaner will formulate a linear programming problem and solve them graphically and simplex method
- The leaner will be able to understand the concepts of duality programming
- The leaner will analyze the different aspects of transportation problems and also assignment problems
- The leaner will develop, organize, evaluate short, long term processes and solve problems
- The leaner will acquire the knowledge of basics in game theory

**Unit 1:** Introduction to convex sets - Mathematical Formulation of LPP - Graphical Solution - Simplex Method – Big M Method - Two Phase Method.

**Unit 2:** Duality in Linear Programming: Formulation of Primal - Dual Pairs - Duality and Simplex Method - Dual Simplex Method.

**Unit 3:** Transportation Problems: Mathematical formulation of the problem - finding initial basic feasible solution using North West Corner Rule and Vogel's approximation method - Moving towards Optimality - Unbalanced Transportation Problems. Assignment Problems: Mathematical formulation of Assignment Problems - Assignment algorithm - Routing Problems.

**Unit 4:** Sequencing Problems: Problems with 'n' jobs and 'k' machines - Problems with 'n' jobs and 2 machines - Problems with 2 jobs and 8 machines - Problems with 2 jobs and 3 machines.

**Unit 5:** Game Theory: Two persons Zero sum games - maximin and minimax principle - Games without saddle points - Mixed strategies - Graphical method - Dominance property.

#### **Text Book:**

1. KantiSwarup, P. K. Gupta& Man Mohan, **Operations Research**, Sultan Chand& Sons, New Delhi, Twelfth Revised Edition, 2005.

Unit 1: chapter 2: 2.1,2.2, chapter 3: 3.2, chapter 4; 4.1, 4.4.

Unit 2: chapter 5: 5.2, 5.3, 5.7, 5.9.

Unit 3: Chapter 10: 10.2,10.9, 10.14, Chapter 11: 11.2, 11.3.

Unit 4: Chapter 12: 12.1 – 12.6.

Unit 5: Chapter 17: 17.1 – 17.7.

- 1. P. K. Gupta & D. S. Hira, **Operations Research**, S. Chand & Company Ltd., New Delhi, 2002.
- 2. J. K. Sharma, **Operations Research theory and its applications**, 2<sup>nd</sup> Edition, Macmillan, New Delhi, 2006.
- 3. R. Panneerselvam, Operations Research, Prentice Hall of India Pvt. Ltd., New Delhi, 2002.

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	Skill Based Elective	Semester V	
15N	ATU05S1	QUANTITATIVE SKILLS	Credits: 2

**Objective:** To impart skills in numerical and quantitative techniques.

**Specific outcome of learning:** The leaner will be

- able to critically evaluate various real life situations by resorting to Analysis of key issues and factors.
- proficient in applying graphs, charts and probability techniques on various problems.
- proficient in the problems on relations, coding and decoding.
- able to demonstrate various principles involved in solving mathematical problems and thereby reducing the time taken for performing job functions.
- able to face interviews.

Unit 1: H.C.F and L.C.M of Numbers- decimal fractions- simplifications- square roots and cube roots- average- Problems on Numbers- Problems on Ages Surds and Indices.

Unit 2: Tabulation- Bar graphs- Pie charts- Line graphs- Permutation and combinations-Probability- true discount- Banker's discount- Heights and distances.

Unit 3: Percentages- Profit and Loss- Ratio-Proportion- Partnership- Chain rule- Time and work- Pipes and cistern-Time and Distances.

Unit 4: Problems on Trains- Boats and Streams- Coding and decoding- Blood Relations-Logical Venn Diagram.

Unit 5: Logical deduction- Alphabet Test- Deriving conclusion from passages- Group discussion (on any current relevant topic).

#### Text Book:

1. R.S. Aggarwal, Quantitative Aptitude, 7th Revised Edition, S. Chand & Company Ltd., New Delhi, 2015.

#### Reference:

1. R.S. Aggarwal, A Modern approach to verbal Reasoning, (Fully solved), Chand & Company Ltd., New Delhi, 2012.

Core Course	Semester VI	
15MATU0614	OPERATIONS RESEARCH	Credits: 4

**Objective:** To impart mathematical modeling skills through operations research techniques. **Specific outcome of learning:** The learner will become proficient in modeling and decision making processes in mathematics and engineering.

- The student will be able to demonstrate knowledge of the major concepts of decision theory and decision making process.
- Students will be able to identify the basic analysis of queuing systems.
- Students will be able to identify the basic analysis of various inventory models.
- The students will acquire the knowledge of system reliability and specific types of simulation.
- The learner will become to understand the role and application of PERT/CPM for project scheduling.

Unit 1: Decision Theory: Introduction – Decision making problem – Decision making process
 Decision making environment – Decision under uncertainty – Decision under risk – Decision tree analysis – Decision making with utilities.

Unit 2: Queuing Theory: Introduction – Queuing system – Characteristics of Queuing system
Probability Distributions in Queuing system – Classification of Queuing Models – Transient
and Steady State. Definitions – Poisson Queuing system.

**Unit 3:** Inventory Control: The inventory decisions – Cost associated with inventories – Factors affecting inventory control – Economic Order Quantity (EOQ) – Deterministic Inventory Problems with no shortages – Deterministic Inventory Problems with shortages – EOQ Problems with Price Breaks.

Unit 4: Replacement Problems and System Reliability: Replacement of equipment – Replacement of equipment that fails suddenly – Reliability and system failure rates. Simulation: Methodology of simulation – simulation models – Event type simulation – Generation of Random Numbers – Monte-Carlo Simulation – Simulation of a Queuing System – Simulation of an inventory System.

**Unit 5:** Network Scheduling by PERT/CPM: Network and basic components – Logical sequencing – Rules for network construction – Critical Path Method – Probability considerations in PERT – Distinctions between PERT and CPM.

#### Text Book:

1. KantiSwarup, P. K. Gupta&Man Mohan, **Operations Research**,Twelfth Revised Edition, Sultan Chand & Sons New Delhi, 2005.

Unit 1: Chapter 16: 16.1-16.8.

Unit 2: Chapter 20: 20.1-20.8.

Unit 3: Chapter 19: 19.1-19.8.

Unit 4: Chapter 18: 18. 1-18.3, 18.6, Chapter 23: 23.1-23.9.

Unit 5: Chapter 21: 21.1-21.7.

- 1. P. K. Gupta & D. S. Hira, **Operations Research**, S. Chand and Company Ltd., New Delhi, 2002.
- 2. J. K. Sharma, **Operations Research theory and its applications**, 2<sup>nd</sup>Edition, Macmillan India Limited, 2003.

Core Course	Semester VI	
15MATU0615	DIFFERENTIAL EQUATIONS	Credits: 4

**Objective:** To introduce the basic concepts of differential equations and Fourier series.

## **Specific outcome of learning:** The learner will

- Understand the basic concepts of first order differential equation and it applications.
- Determine solutions to second order linear homogeneous, non-homogeneous differential equations with constant coefficients.
- Find solutions by applying Laplace transform methods.
- Understand the elementary theory of partial differential equations, and solve it using various techniques.
- Familiar with Fourier series and their applications to partial differential equations.

**Unit 1:** Differential Equations: Introduction – First order O.D.E – Types of first order O.D.E – Applications of first order O.D.E – first order O.D.E of higher degree.

**Unit 2:** Linear Second Order Equations with constant coefficient and particular integral of the functions of the type  $X^m$ ,  $e^{ax}cosbx$  and  $e^{ax}sin$  bx only. Homogeneous linear equations with variable coefficients - Variation of parameters - Simultaneous Equations - Linear equations of the second order with variable coefficients.

**Unit 3:** Laplace Transform of Elementary Functions - Laplace Transforms of Periodic Functions - Inverse Transforms - Solutions of Ordinary Second Order Differential Equations with Constant Coefficients.

**Unit 4:** Partial Differential Equations (PDE) Forming a PDE - Lagrange Method of solving Linear Equations - Standard forms of PDE - Charpits Method.

**Unit 5:** Fourier series: Expansion of a function - Drichlet's Conditions - Determining the Fourier Coefficients- Odd and Even Functions - Half Range Sine Series - Half Range Cosine Series.

#### **Text Books:**

1. S. Narayanan &T.K. ManickavasagamPillai, **Differential Equations**, S. Viswanathan Pvt. Ltd., Chennai, 1995.

Unit 1: Chapters I-IV

Unit 2: Chapter V (up to section 6), Chapter VI, Chapter VIII.

Unit 3: Chapter IX

Unit 4: Chapter XII

2. T. Veerarajan, **Transforms and Partial Differential Equations**, Tata McGraw Hill Education Private Ltd., New Delhi, 2012.

Unit 5: Chapter 1-Section 1.1 - 1.9

- 1. Arumugam& Isaac, **Differential Equations and Applications**, New Gamma Publishing House, 2003.
- 2. M. D. Raisinghania, **Advanced Differential equations**, S. Chand Publications, New Delhi 2004.
- 3. K. Vairaamanickam, Nirmala P. Ratchagar& T. Tamilselvan, **Transforms and Partial Differential Equations,** SciTech Publications Pvt. Ltd., 2011.

Core Course	Semester VI	
15MATU0616	COMPLEX ANALYSIS	Credits: 4

**Objective:** To introduce the concepts of complex numbers and analytic functions.

# Specific outcome of learning:

- The learner will acquire basic concepts of analytic function and its properties
- The learner will acquire basic knowledge about conformal and bilinear transformation
- The learner will gain knowledge of integration of complex valued function
- The learner will become proficient in series of analytic function
- The learner will acquire skills of finding integral values of complex function using residues

**Unit 1:** Analytic function - Cauchy Riemann Equation in Cartesian and polar co-ordinates - Harmonic function Properties and applications.

**Unit 2:** Conformal mappings - Linear and Non-linear transformations - Bilinear transformations - Properties and applications.

**Unit 3:** Integration in the Complex plane - Cauchy's Integral theorem - Cauchy's Integral formula - Liouville's theorem - Maximum modulus theorem - Applications and simple problems.

Unit 4: Taylor's and Laurent's series - Expansion of functions in power series - Singular pointsTypes of singularities - Properties of singularities - Identification of singularities.

**Unit 5:** Calculus of Residues: Residue theorem - Integration of functions of the typeinvolving  $\cos x$ ,  $\sin x$  — Applications and problems relating to residues.

#### **Text Book:**

1. S. Narayanan & T.K. ManickavasagamPillai, **Complex Analysis**, S. Viswanathan Publishers, Chennai, 1997.

Unit 1: Chapter 1

Unit 2: Chapter 2

Unit 3: Chapter 3

Unit 4: Chapter 4 Unit 5: Chapter 5

- 1. S. Arumugam, A. Thangapandi Isaac& A. Somasundaram, **Complex Analysis**, SciTech Publications, India, Pvt. Ltd., 2004.
- 2. S. Ponnusamy, **Foundations of Complex Analysis**, 2<sup>nd</sup>Edition, Narosa Publication, New Delhi, 2005.
- 3. R. V. Churchill &J.W.Brown, **Complex variables and applications**, 5<sup>th</sup>Edition, McGraw Hill, Singapore, 1990.

Core Course	Semester VI	
15MATU0617	GRAPH THEORY	Credits: 3

**Objective:** To acquire knowledge of different types of graphs.

# Specific outcome of learning:

- To understand different Models of a graph
- Students can develop various algorithms related to graph parameters
- To understand how to solve different real life problems
- To understand many techniques to solve a particular problem
- To understand different colouring parameters.

**Unit 1:** The Definition of a graph - graphs as models - more definitions - vertex degrees, sub graphs - paths and cycles - Matrix representation of graphs - fusions. Trees and Connectivity - definitions and simple properties – bridges - spanning trees.

**Unit 2:** Connector problems - Kruskal's algorithm - Prim's algorithm - Shortest path problems- Cut vertices and connectivity.

**Unit 3:** Euler tours and Hamiltonian cycles - The Chinese postman problem - Fleury's Algorithm - Hamiltonian Graphs - The travelling salesman problems (Except closest insertion Algorithm).

**Unit 4:** Matching and Augmenting paths - The marriage problem - The Hall's marriage theorem - The Personnel Assignment Problem - The Optimal Assignment Problem.

**Unit 5:** Plane and Planar Graphs - Euler's Formula - Vertex colouring - Vertex colouring Algorithms - critical graphs.

### **Text Book:**

J.Clark &D.A.Holton, **A first Look at Graph Theory**, Allied Publishers, New Delhi,1995. Chapters 1,2,3,4,5 and 6.

- 1. J.A. Bondy & U.S.R.Murty, **Graph Theory with Applications**, Elsevier, New York, 1976.
- 2. S.A.Choudam, A first course in Graph Theory, Macmillian, India Ltd., Delhi, 2007.

Modular Course	Semester VI	
15MATU06M1	FUZZY SET THEORY	Credits: 2

**Specific outcome of learning:** The learner will be able to

- recognize the concept of fuzzy sets and its properties.
- distinguish fuzzy sets from crisp sets.
- perform various operations on fuzzy sets.
- understand the fuzzy graphs and fuzzy relations.

**Unit 1:** Fuzzy Sets: Sets- Definition of Fuzzy - Expanding Concepts of Fuzzy Set -Standard Operation of Fuzzy Set- Fuzzy Complement - Fuzzy Union- Fuzzy Intersection - Other Operations in Fuzzy Set - T-norms and T-conorms.

**Unit 2:** Fuzzy Relation and Composition: Fuzzy Relation—Extension of Fuzzy set - Fuzzy Graph and Relation: Fuzzy Graph — Characteristics of Fuzzy Relation—Classification of Fuzzy Relation—Other Fuzzy Relations.

#### Text Book:

1. Kwang H. Lee, First Course on Fuzzy Theory and Applications, Springer, New York, 2005.

Unit 1: Chapter 1: Sections 1.4 -1.6; Chapter 2: Sections 2.1 - 2.6

Unit 2: Chapter 3: Sections 3.3 - 3.4; Chapter 4: Sections 4.1 - 4.4

- 1. G. J. Klir and B. Yuan, Fuzzy Sets and Fuzzy Logic, Prentice-Hall India, 1995.
- 2. H. J. Zimmermann, Fuzzy Set Theory and Its Applications, Springer, 2001.
- 3. Didier Dubois and Henri Prade, **Fuzzy Sets and Systems: Theory and Applications**, Academic Press, 1980.

Modular Course	Semester VI	`
15MATU 06M2	MATHEMATICAL SKILLS	Credits: 2

**Objective:** To impart Mathematical competitive skills.

# Specific outcome of learning:

- The learner will acquire knowledge of interest calculation.
- The learner will become proficient in odd man out and series problems.

**Unit 1:** Allegation or mixture – Simple Interest – Compound Interest – Area

Unit 2: Volume and surface Areas - Calendar - Odd man out and series

# **Text Books:**

1.R.S.Aggarwal, **Quantitative Aptitude**, 7<sup>th</sup> Revised Edition, S. Chand and Company Ltd, New Delhi, 2015

Unit 1: Section1, Topic 20,21,22,24 Unit 2: Section1, Topic 25, 27, 35

#### Reference:

1. Abhijit Guha, **Quantitative Aptitude for MBA Entrance Examinations**, Tata McGraw-Hill Publishing Company Ltd, New Delhi, 2006

Modular Course	Semester VI	
15MATU 06M3	ADVANCED STATISTICS	Credits: 2

**Objective:** To import skills of various advanced statistical techniques.

# Specific outcome of learning

- The learner will become proficient in consistency of data and index number.
- The learner will acquire knowledge of measuring trends and analysis of variance.

**Unit 1: Theory Attributes:** Attributes-Consistency of data- Independent and Association of data- Index Number: Types of index numbers- Conversion of chain base to fixed base and converse.

**Unit 2: Analysis of Time series:** Components of time series- Measurement of trends-Analysis of variance: One, Two, Three Criteria classification

#### Text Book:

S. Arumugam & A. Thangapandi Isaac, Statistics, New Gamma Publishing house, Tirunelveli, 2006.

Unit 1: Chapters 8, 9, Unit 2: Chapters 10, 11

- 1. J. N. Kapoor & V. C. Saxena, **Mathematics Statistics**, S. Chand & Co Pvt. Ltd, Newdelhi, 1994.
- **2.** S. C. Gupta & V.K. Kapoor, **Fundamentals of Mathematical Statistics,** S.Chand & & Co Pvt. Ltd, Newdelhi, 1994.

Core Course		
15MATU0618	PROJECT	Credits: 4

Major Elective	Semester IV	
15MATU04E1	NUMERICAL METHODS	Credits: 3

**Objective:** To develop efficient algorithms for solving problems in Science, Engineering and Technology.

# Specific outcome of learning:

- The learner will capable of solving the interpolation problems.
- Students will be able to identify the basic concept of numerical differentiation and integration, principle of least squares.
- The leaner will analyze the different aspects of numerical solution of algebraic and transcendental equations.
- The learner will become knowledgeable in solving solution to simultaneous linear equations.
- The learner will become to understand the role and application of nnumerical solution of ordinary differential equations.

**Unit-1:** Errors in Numerical Calculations: Errors and their computations - A general error formula - Error in a series. Approximation Solution of Algebraic and Transcendental equations: The Bisection method – The Method of False position - Iteration method - Newton - Raphson method.

**Unit-2:** Interpolation: Finite differences - Forward Differences - Backward Differences - Central Differences - Symbolic Relations and Separation of Symbols. Newton's Formulae for Interpolation - Gauss's central difference formulae - Stirling's formula - Interpolation with unevenly spaced points: Lagrange's interpolation formula - Inverse Interpolation.

**Unit-3:** Numerical Differentiation: Derivatives using Newton's Forward Difference Formula – Derivatives using Newton's Backward Difference Formula - Derivatives using Stirling's Formula - Maxima and Minima of Tabulated Function. Numerical Integration: General Quadrature Formula - Trapezoidal Rule - Simpson's 1/3 Rule - Simpson's 3/8 Rule.

**Unit-4:** Numerical Solutions of System of Linear Equations: Gauss elimination method - Gauss - Jordan method - Jacobi's method - Gauss - Seidel method.

**Unit -5:** Numerical Solutions of Ordinary Differential Equations: Solution by Taylor's series - Picard's method of successive approximations – Runge - Kutta Methods - Milne's Predictor - Corrector Method.

# **Text Book:**

1. S. S. Sastry, **Introductory Methods of Numerical Analysis**, Fourth Edition, Prentice Hall of India Pvt. Ltd., New Delhi, 2005.

Unit 1: Chapter 1: Section 1.3 to 1.5, Chapter 2: Section 2.1 to 2.5

Unit 2: Chapter 3: Section 3.3.1 to 3.3.4, 3.6, 3.7.1, 3.7.2, 3.3.9

Unit 3: Chapter 5: Section 5.1, 5.2.1, 5.3, 5.4.1, 5.4.2, 5.4.3

Unit 4: Chapter 6: Section 6.3.2, 6.3.3, 6.4

Unit 5: Chapter 7: Section 7.2, 7.3, 7.5, 7.6

- 1. Gerald &Wheatly, **Applied Numerical Analysis**, Sixth Edition, Pearson Education Pvt. Ltd., New Delhi, 2002.
- 2. S. Arumugam, A. Thangapandi Isaac & A. Somasundaram, **NumericalMethods**, Scitech Publications Pvt. Ltd., 2001.
- 3. V. N. Vedamurthy&N. Ch. S. N. Iyengar, **Numerical Methods**, Vikas Publishing House Pvt. Ltd. New Delhi, 2000.

Major Elective	Semester IV	
15MATU04E2	FINANCIAL MATHEMATICS	Credits: 3

**Objective:** To impart mathematical concepts related to finance and insurance.

# Specific outcome of learning:

- Specialise advanced topics in the area of financial mathematics and actuarial analysis and their applications
- Differentiate between simple and compound interest and extrapolate the advantages and disadvantages of each in specific situations
- Do calculations using computational tools efficiently and correctly and verify solutions in terms of the context.
- Use solutions to calculations effectively to define the changes that occur over a period.
- Students will use methods of correlation and regression to analyse and interpret a given data set and make predictions.

**Unit 1:** Mathematics of Compound interest - Mathematical base of life contingencies - effective interest rate, nominal interest rate - continuous payments, interest in advance - perpetuities - annuities - repayment of debit- internal rate of return future life time of a life aged x - the model - force of mortality - analytical distribution of T - the curate future life time of T - Life table -Probabilities of deaths for fraction of a year.

**Unit 2:** Life insurance - insurance types - whole life and term insurance - pure Endowment - Endowments - insurance, payable at the moment of death- general type of life insurance - variable life insurance - recursive formula. Life annuities - elementary life annuities - payment made more frequently than once a year - variables life annuities - types of life annuities - recursive formula - inequalities - Payment starting at non-integral age. Net premium - elementary forms of insurance - whole life - Term insurance, pure Endowment - Endowments - deferred life annuities - premium paid m times year - general type of life insurance - policies with premium refund - stochastic interest.

**Unit 3:** Net premium reserves - examples - recursive consideration - survival risk - net premium risk of a whole life insurance - net premium reserve at fractional duration - allocations of overall loss to policy year - conversion of an insurance - Technical gain - procedure for pure endowment - continuous model - multiple decrements model - forces of decrement - curate life time of (x), general type of insurance, net premium reserve - continuous model. Multiple life insurance - Joint life status - simplification- last survivor status general symmetric status - Schuette-Nesbitt formula - asymmetric annuities-asymmetric insurances.

**Unit 4:** The total claim amount in a portfolio - normal approximations - calculation of total claim amount distribution - compound Poisson approximation - recursive calculation of compound Poisson distribution - reinsurance stop-loss reinsurance - expense loading - introduction expenses loaded premium - expense loaded premium reserves - estimating probabilities of death - problem description - classical method - Alternative solution - maximum likelihood method - statistical inference - Bayesian approach - multiple causes of decrement - interpretation of result.

**Unit 5:** Applications in regression analysis - Functional form -dummy variable - distributed log model - forecasting - binary choice model - interpretation of binary choice model - solved problems.

#### Text Books:

- 1. Hans U.Gerber, **Life Insurance Mathematics**, Third edition, Springer Verlag, New York 1997. Chapters: 1-ll.
- 2. D.Salvalore & D.Reagle, **Statistics and Economics**, Schaum's outline Series, Tata McGraw Hill, New Delhi, 2005. Chapter 8 only.

Major Elective	Semester V	
15MATU05E1	DISCRETE MATHEMATICS	Credits: 3

**Objective:** To impart theoretical knowledge about discrete mathematics.

# Specific outcome of learning:

- Formulate and interpret statements presented in Boolean logic. Reformulate statements from common language to formal logic. Apply truth tables and the rules of propositional and predicate calculus,
- Formulate short proofs using the following methods: direct proof, indirect proof, proof by contradiction, and case analysis,
- Demonstrate a working knowledge of set notation and elementary set theory, recognize the connection between set operations and logic, prove elementary results involving sets, and explain Russell's paradox,
- Apply the different properties of injections, surjections, bijections, compositions, and inverse functions,
- Solve discrete mathematics problems that involve: computing permutations and combinations of a set, fundamental enumeration principles, and graph theory.
- **Unit 1:** Mathematical Logic- Propositional calculus- Basic Logical operators- conditional statements- Bi conditional statement- tautologies- contradictions- equivalence implications.
- **Unit 2:** Norms forms- Theory of inference for the statement calculus- The predicate calculus-inference theory and predicate calculus.
- **Unit 3:** Recurrence relations and generating functions- recurrence relation- solution of linear recurrence relation with constant coefficients- Non homogeneous recurrence relations-solution of Non homogeneous recurrence relations- Methods of generating functions.
- **Unit 4:** Basic theorems on Boolean Algebra- Duality principle Boolean functions.
- **Unit 5:** Boolean functions- Applications of Boolean algebra- Logic gates and circuits-combinatorial circuits- Boolean expression karnaugh map.

# Text Book:

1. M.K. Venkatraman, N.Sridharan& N.Chandrasekaran, **Discrete Mathematics**, The National Publishing company India, 2000.

- 1. J.B.Tremblay, R. Manohar, **Discrete Mathematical structures with applications to computer Science**, Tata McGraw Hill, International edition New Delhi:1997, Reprint 2007.
- 2. K.D.Joshi, Foundations of Discrete Mathematics, New Age International, New Delhi.
- 3. SartajSahni, Concepts in discrete Mathematics, Narosa Publishing House, New Delhi.
- 4. Garrett Birkhoff Thomas C. Bartee, Modern Applied Algebra, CBS Publishers, New Delhi.

Major Elective	Semester V	
15MATU05E2	INTRODUCTION TO ACTUARIAL SCIENCE	Credits: 3

**Objective:** To impart various concepts related to insurance.

# Specific outcome of learning:

- Develop an understanding of the actuarial profession, what actuaries do, and how they do it.
- How liabilities in general insurance and life insurance are modelled and evaluated.
- why life insurance is so different and more predictable and despite
- Develop the critical and analytical thinking skills necessary for success in the profession.
- application of quantitative skills to problems in finance that normally involve risk or uncertainty.

**Unit 1:** The widening scope of Actuarial Theory and practice: Introduction – Financial Intermediaries -their role in resolving the "constitutional weakness" - Functional Approach to the Analysis of Intermediaries - Intermediating function If Banks, insurance, unit Trust and mutual funds. Banks, Insurance Companies and Pension Funds: Fundamental Similarities and Differences- Banks loans, Credit Risk and Insurance -The Evolving Relationship Banking and Insurance - Some examples of the Evolving Product Links between Banks and Non-banks – conclusion.

**Unit 2:** Investment and Valuation: Introduction-Cash Instruments-General Characteristics-Specific Cash instruments and Valuation Issues-Risk Characteristics – General Characteristics of conventional Bonds- Government Bonds-Corporate Bonds – Bond Valuation- Economic Analysis-Risk Characteristics-General Characteristics of Index Linked Bonds - Valuation - Economic Analysis - Risk Characteristics – Estimating Market Expectations of Inflation using Market Information.

**Unit 3:** General Characteristics of Foreign Currency Bonds: Valuation-Economic Analysis - Risk Characteristics. General Characteristics of Equity Investment: Equity Valuation-Economic Analysis - Risk Analysis. Real Estate Investment: Valuation - Economic Analysis - Risk Analysis. International Equity Investment: International Equity Valuation - Economic Analysis - Risk Analysis - Derivatives - General Characteristics - Valuation - Risk Characteristics.

**Unit 4:** Investment Risk: Introduction-Utility theory and Risk measures - Relating Utility Functions to Risk Aversion and the Risk Premium -Summary Risk Measures - Standard Deviation of Returns- Downside/Shortfall Risk Measures-Value at Risk-Practical Issues when Calculating VAR- Tail Loss-Combining Risk and Return Measures - Coherent Risk Measures-The use of Shortfall Constraints.

**Unit 5:** Portfolio selection Techniques and Investment Modeling: Introduction – Immunization - Derivation of Conditions - Observation on the Theory of Immunization-The usefulness of Immunization in Practice-Modern Portfolio Theory – Portfolio Diversification-Efficient Portfolios-Capital Market Line- The Capital Asset Pricing Model. Modern Portfolio Theory: Insights and Limitations - Extension of Portfolio Theory to Include Actuarial Liabilities-Portfolio Optimization in the Presence of Liabilities-Connection between Redington and the Wise-Willkie Approach-Generalization of Portfolio Optimization in the Presence of Liabilities-Portfolio Selection in an Asset/Liability Framework using a Generalized Approach to Risk.

#### Text Book:

1. Philip Booth, **Modern Actuarial Theory and Practice**, Second Edition, Chapman and Hall / CRC, New York, 2004. Chapter 1: Secs1.1 to. 1.11, Chapter 2: Secs2.1 to 2.9, Chapter 4: Secs4.1 to 4.6, Chapter 5: Secs5.1 to 5.4.